

# Example evaluation of FOCUS dataset Z

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**Key words:** Kinetics, FOCUS, nonlinear optimisation

## 1 The data

The following code defines the example dataset from Appendix 7 to the FOCUS kinetics report ([FOCUS Work Group on Degradation Kinetics, 2011](#)), p.350.

```
require(mkin)
LOD = 0.5
FOCUS_2006_Z = data.frame(
  t = c(0, 0.04, 0.125, 0.29, 0.54, 1, 2, 3, 4, 7, 10, 14, 21,
        42, 61, 96, 124),
  Z0 = c(100, 81.7, 70.4, 51.1, 41.2, 6.6, 4.6, 3.9, 4.6, 4.3, 6.8,
        2.9, 3.5, 5.3, 4.4, 1.2, 0.7),
  Z1 = c(0, 18.3, 29.6, 46.3, 55.1, 65.7, 39.1, 36, 15.3, 5.6, 1.1,
        1.6, 0.6, 0.5 * LOD, NA, NA, NA),
  Z2 = c(0, NA, 0.5 * LOD, 2.6, 3.8, 15.3, 37.2, 31.7, 35.6, 14.5,
        0.8, 2.1, 1.9, 0.5 * LOD, NA, NA, NA),
  Z3 = c(0, NA, NA, NA, NA, 0.5 * LOD, 9.2, 13.1, 22.3, 28.4, 32.5,
        25.2, 17.2, 4.8, 4.5, 2.8, 4.4))

FOCUS_2006_Z_mkin <- mkin_wide_to_long(FOCUS_2006_Z)
```

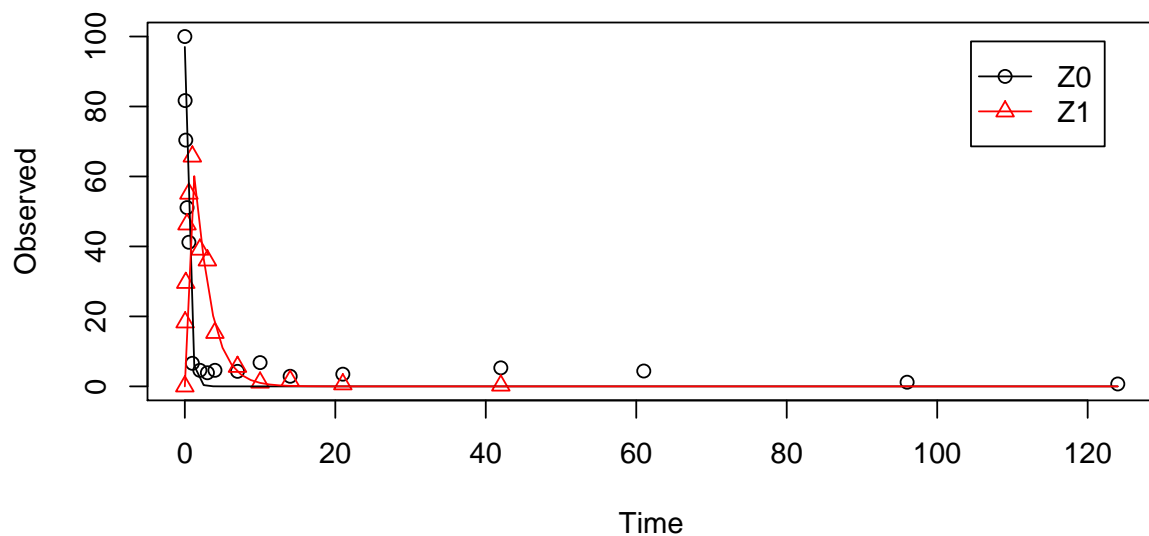
## 2 Parent compound and one metabolite

The next step is to set up the models used for the kinetic analysis. As the simultaneous fit of parent and the first metabolite is usually straightforward, Step 1 (SFO for parent only) is skipped here. We start with the model 2a, with formation and decline of metabolite Z1 and the pathway from parent directly to sink included (default in mkin).

```

Z.2a <- mkinmod(Z0 = list(type = "SF0", to = "Z1"),
               Z1 = list(type = "SF0"))
m.Z.2a <- mkinfit(Z.2a, FOCUS_2006_Z_mkin, quiet = TRUE)
plot(m.Z.2a)

```



```

summary(m.Z.2a, data = FALSE)

## mkin version:      0.9.34
## R version:        3.1.2
## Date of fit:       Fri Nov 21 19:18:59 2014
## Date of summary:   Fri Nov 21 19:18:59 2014
##
## Equations:
## d_Z0 = - k_Z0_sink * Z0 - k_Z0_Z1 * Z0
## d_Z1 = + k_Z0_Z1 * Z0 - k_Z1_sink * Z1
##
## Model predictions using solution type eigen
##
## Fitted with method Port using 349 model solutions performed in 4.396 s
##
## Weighting: none
##
## Starting values for parameters to be optimised:
##          value      type

```

```

## Z0_0      100.0000  state
## k_Z0_sink  0.1000 deparm
## k_Z0_Z1    0.1001 deparm
## k_Z1_sink  0.1002 deparm
##
## Starting values for the transformed parameters actually optimised:
##              value lower upper
## Z0_0          100.000000  -Inf  Inf
## log_k_Z0_sink -2.302585  -Inf  Inf
## log_k_Z0_Z1   -2.301586  -Inf  Inf
## log_k_Z1_sink -2.300587  -Inf  Inf
##
## Fixed parameter values:
##      value  type
## Z1_0      0  state
##
## Optimised, transformed parameters:
##              Estimate Std. Error Lower Upper t value Pr(>|t|) Pr(>t)
## Z0_0          97.0100          NA     NA     NA     NA      NA      NA
## log_k_Z0_sink -21.9100          NA     NA     NA     NA      NA      NA
## log_k_Z0_Z1    0.8047          NA     NA     NA     NA      NA      NA
## log_k_Z1_sink  -0.7296          NA     NA     NA     NA      NA      NA
##
## Parameter correlation:
## Could not estimate covariance matrix; singular system:
##
## Residual standard error: 5.064 on 27 degrees of freedom
##
## Backtransformed parameters:
##              Estimate Lower Upper
## Z0_0          9.701e+01     NA     NA
## k_Z0_sink  3.061e-10      NA     NA
## k_Z0_Z1    2.236e+00      NA     NA
## k_Z1_sink  4.821e-01      NA     NA
##
## Chi2 error levels in percent:
##              err.min n.optim df
## All data    17.89      4 26
## Z0          18.04      3 14
## Z1          15.08      1 12
##
## Resulting formation fractions:

```

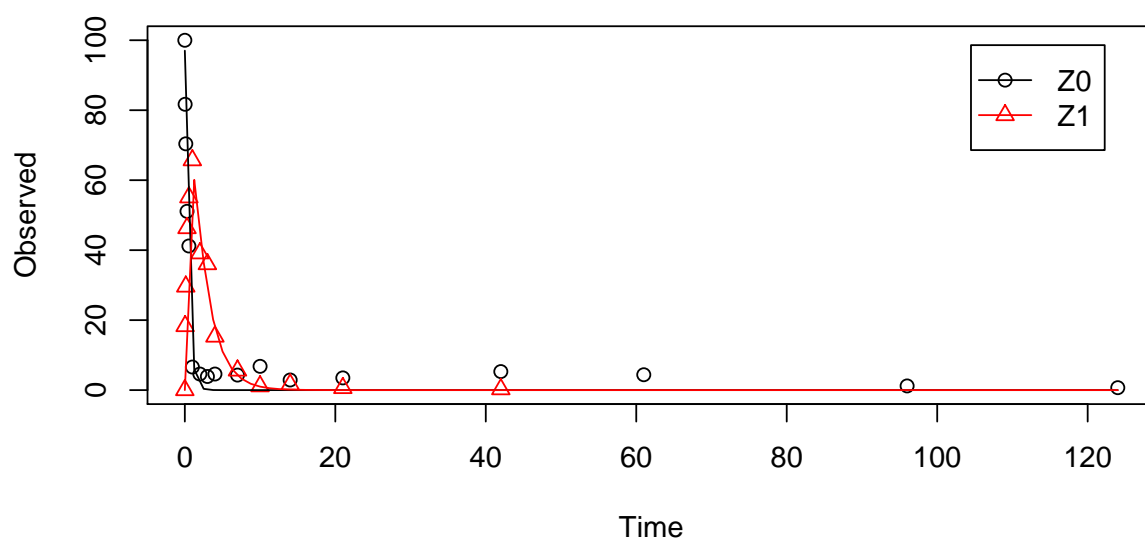
```
##          ff
## Z0_sink 1.369e-10
## Z0_Z1   1.000e+00
## Z1_sink 1.000e+00
##
## Estimated disappearance times:
##      DT50 DT90
## Z0 0.310 1.030
## Z1 1.438 4.776
```

As obvious from the summary, the kinetic rate constant from parent compound Z to sink is negligible. Accordingly, the exact magnitude of the fitted parameter  $\log k_{Z\_sink}$  is ill-defined and the covariance matrix is not returned. This suggests, in agreement with the analysis in the FOCUS kinetics report, to simplify the model by removing the pathway to sink.

A similar result can be obtained when formation fractions are used in the model formulation:

```
Z.2a.ff <- mkinmod(Z0 = list(type = "SFO", to = "Z1"),
                  Z1 = list(type = "SFO"),
                  use_of_ff = "max")

m.Z.2a.ff <- mkinfit(Z.2a.ff, FOCUS_2006_Z_mkin, quiet = TRUE)
plot(m.Z.2a.ff)
```



```
summary(m.Z.2a.ff, data = FALSE)

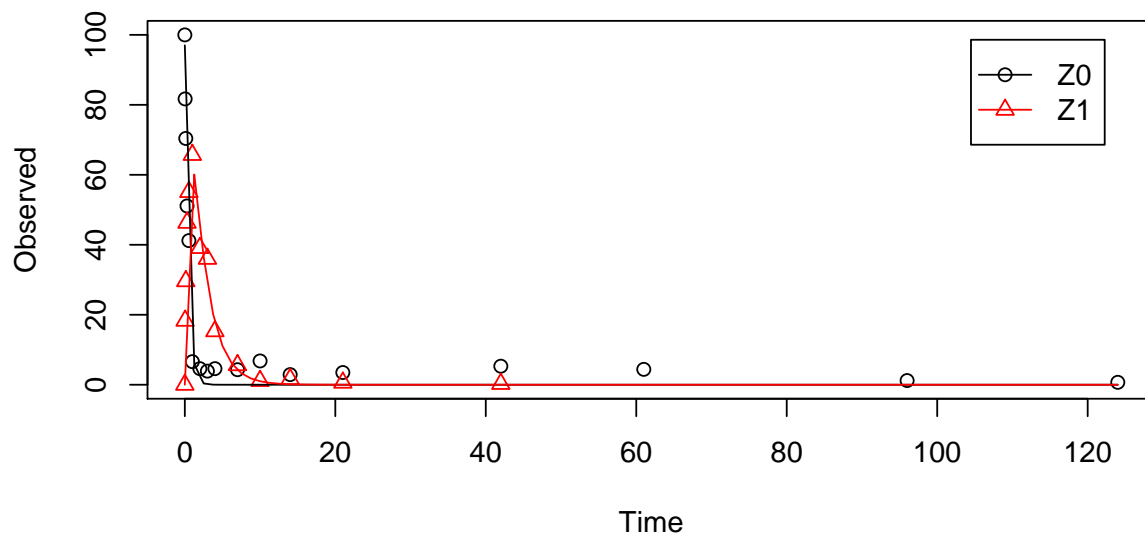
## mkin version:      0.9.34
## R version:        3.1.2
## Date of fit:       Fri Nov 21 19:19:03 2014
## Date of summary:  Fri Nov 21 19:19:03 2014
##
## Equations:
## d_Z0 = - k_Z0 * Z0
## d_Z1 = + f_Z0_to_Z1 * k_Z0 * Z0 - k_Z1 * Z1
##
## Model predictions using solution type eigen
##
## Fitted with method Port using 329 model solutions performed in 4.171 s
##
## Weighting: none
##
## Starting values for parameters to be optimised:
##           value   type
## Z0_0       100.0000 state
## k_Z0        0.1000 deparm
## k_Z1        0.1001 deparm
## f_Z0_to_Z1  0.5000 deparm
##
## Starting values for the transformed parameters actually optimised:
##           value lower upper
## Z0_0       100.000000  -Inf   Inf
## log_k_Z0    -2.302585  -Inf   Inf
## log_k_Z1    -2.301586  -Inf   Inf
## f_Z0_ilr_1   0.000000  -Inf   Inf
##
## Fixed parameter values:
##           value   type
## Z1_0         0 state
##
## Optimised, transformed parameters:
##           Estimate Std. Error Lower Upper t value Pr(>|t|) Pr(>t)
## Z0_0           97.0100         NA    NA    NA    NA      NA    NA
## log_k_Z0        0.8047         NA    NA    NA    NA      NA    NA
## log_k_Z1       -0.7296         NA    NA    NA    NA      NA    NA
## f_Z0_ilr_1     15.8900         NA    NA    NA    NA      NA    NA
##
```

```
## Parameter correlation:
## Could not estimate covariance matrix; singular system:
##
## Residual standard error: 5.064 on 27 degrees of freedom
##
## Backtransformed parameters:
##           Estimate Lower Upper
## Z0_0       97.0100    NA    NA
## k_Z0        2.2360    NA    NA
## k_Z1        0.4821    NA    NA
## f_Z0_to_Z1  1.0000    NA    NA
##
## Chi2 error levels in percent:
##           err.min n.optim df
## All data   17.89      4 26
## Z0         17.56      2 15
## Z1         15.59      2 11
##
## Resulting formation fractions:
##           ff
## Z0_Z1    1.00e+00
## Z0_sink 1.73e-10
##
## Estimated disappearance times:
##      DT50  DT90
## Z0 0.310 1.030
## Z1 1.438 4.776
```

Here, the ilr transformed formation fraction fitted in the model takes a very large value, and the backtransformed formation fraction from parent Z to Z1 is practically unity. Again, the covariance matrix is not returned as the model is overparameterised.

The simplified model is obtained by setting the list component `sink` to `FALSE`.

```
Z.3 <- mkinmod(Z0 = list(type = "SFO", to = "Z1", sink = FALSE),
              Z1 = list(type = "SFO"), use_of_ff = "max")
m.Z.3 <- mkinfit(Z.3, FOCUS_2006_Z_mkin, quiet = TRUE)
plot(m.Z.3)
```



```
summary(m.Z.3, data = FALSE)

## mkin version:    0.9.34
## R version:      3.1.2
## Date of fit:     Fri Nov 21 19:19:04 2014
## Date of summary: Fri Nov 21 19:19:04 2014
##
## Equations:
## d_Z0 = - k_Z0 * Z0
## d_Z1 = + k_Z0 * Z0 - k_Z1 * Z1
##
## Model predictions using solution type eigen
##
## Fitted with method Port using 100 model solutions performed in 1.249 s
##
## Weighting: none
##
## Starting values for parameters to be optimised:
##      value   type
## Z0_0 100.0000 state
## k_Z0  0.1000 deparm
## k_Z1  0.1001 deparm
##
## Starting values for the transformed parameters actually optimised:
```



```

##           value lower upper
## Z0_0      100.000000 -Inf   Inf
## log_k_Z0  -2.302585 -Inf   Inf
## log_k_Z1  -2.301586 -Inf   Inf
##
## Fixed parameter values:
##       value type
## Z1_0      0 state
##
## Optimised, transformed parameters:
##       Estimate Std. Error   Lower   Upper t value Pr(>|t|)
## Z0_0       97.0100    2.68200 91.5200 102.5000  36.18 4.727e-25
## log_k_Z0    0.8047    0.06568  0.6702   0.9392  12.25 9.117e-13
## log_k_Z1   -0.7296    0.08854 -0.9109  -0.5482  -8.24 5.738e-09
##           Pr(>t)
## Z0_0       2.364e-25
## log_k_Z0   4.558e-13
## log_k_Z1   2.869e-09
##
## Parameter correlation:
##           Z0_0 log_k_Z0 log_k_Z1
## Z0_0       1.0000  0.10629  0.41038
## log_k_Z0   0.1063  1.00000  0.04345
## log_k_Z1   0.4104  0.04345  1.00000
##
## Residual standard error: 4.973 on 28 degrees of freedom
##
## Backtransformed parameters:
##       Estimate   Lower   Upper
## Z0_0   97.0100 91.5200 102.500
## k_Z0    2.2360  1.9550  2.558
## k_Z1    0.4821  0.4022  0.578
##
## Chi2 error levels in percent:
##       err.min n.optim df
## All data   17.61      3 27
## Z0         17.56      2 15
## Z1         15.08      1 12
##
## Estimated disappearance times:
##       DT50 DT90
## Z0 0.310 1.030

```

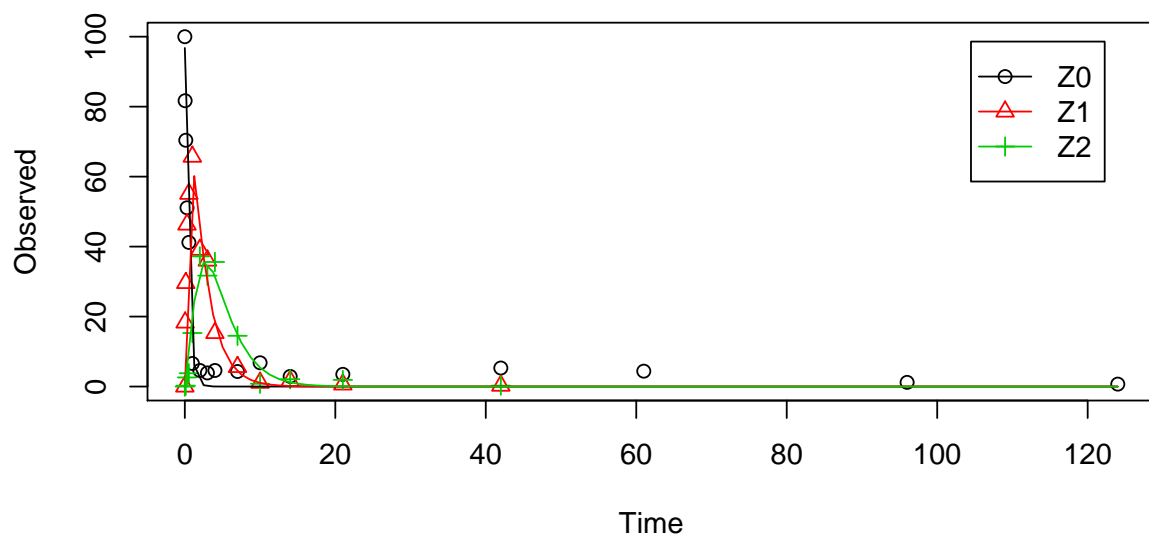
```
## Z1 1.438 4.776
```

As there is only one transformation product for Z0 and no pathway to sink, the formation fraction is internally fixed to unity.

### 3 Including metabolites Z2 and Z3

As suggested in the FOCUS report, the pathway to sink was removed for metabolite Z1 as well in the next step. While this step appears questionable on the basis of the above results, it is followed here for the purpose of comparison. Also, in the FOCUS report, it is assumed that there is additional empirical evidence that Z1 quickly and exclusively hydrolyses to Z2.

```
Z.5 <- mkinmod(Z0 = list(type = "SF0", to = "Z1", sink = FALSE),  
              Z1 = list(type = "SF0", to = "Z2", sink = FALSE),  
              Z2 = list(type = "SF0"))  
m.Z.5 <- mkinfit(Z.5, FOCUS_2006_Z_mkin, quiet = TRUE)  
plot(m.Z.5)
```



```
summary(m.Z.5, data = FALSE)  
## mkin version: 0.9.34  
## R version: 3.1.2
```

```

## Date of fit:      Fri Nov 21 19:19:08 2014
## Date of summary: Fri Nov 21 19:19:08 2014
##
## Equations:
## d_Z0 = - 0 - k_Z0_Z1 * Z0
## d_Z1 = + k_Z0_Z1 * Z0 - 0 - k_Z1_Z2 * Z1
## d_Z2 = + k_Z1_Z2 * Z1 - k_Z2_sink * Z2
##
## Model predictions using solution type eigen
##
## Fitted with method Port using 201 model solutions performed in 3.874 s
##
## Weighting: none
##
## Starting values for parameters to be optimised:
##           value  type
## Z0_0      100.0000 state
## k_Z0_Z1    0.1000 deparm
## k_Z1_Z2    0.1001 deparm
## k_Z2_sink  0.1002 deparm
##
## Starting values for the transformed parameters actually optimised:
##           value lower upper
## Z0_0      100.000000 -Inf  Inf
## log_k_Z0_Z1 -2.302585 -Inf  Inf
## log_k_Z1_Z2 -2.301586 -Inf  Inf
## log_k_Z2_sink -2.300587 -Inf  Inf
##
## Fixed parameter values:
##           value  type
## Z1_0        0 state
## Z2_0        0 state
##
## Optimised, transformed parameters:
##           Estimate Std. Error  Lower  Upper t value Pr(>|t|)
## Z0_0          96.7700    2.26600  92.1900 101.3000  42.710 5.434e-35
## log_k_Z0_Z1     0.7948    0.05843   0.6767   0.9129  13.600 1.361e-16
## log_k_Z1_Z2    -0.7410    0.06821  -0.8789  -0.6032 -10.860 1.682e-13
## log_k_Z2_sink  -0.8027    0.11090  -1.0270  -0.5785  -7.237 8.786e-09
##           Pr(>t)
## Z0_0          2.717e-35
## log_k_Z0_Z1    6.804e-17

```

```

## log_k_Z1_Z2    8.409e-14
## log_k_Z2_sink 4.393e-09
##
## Parameter correlation:
##           Z0_0 log_k_Z0_Z1 log_k_Z1_Z2 log_k_Z2_sink
## Z0_0          1.00000    0.05781    0.28748    0.31786
## log_k_Z0_Z1    0.05781    1.00000   -0.04361    0.01213
## log_k_Z1_Z2    0.28748   -0.04361    1.00000    0.24019
## log_k_Z2_sink  0.31786    0.01213    0.24019    1.00000
##
## Residual standard error: 4.486 on 40 degrees of freedom
##
## Backtransformed parameters:
##           Estimate      Lower      Upper
## Z0_0          96.7700  92.1900 101.3000
## k_Z0_Z1        2.2140   1.9670   2.4920
## k_Z1_Z2        0.4766   0.4152   0.5471
## k_Z2_sink      0.4481   0.3581   0.5607
##
## Chi2 error levels in percent:
##           err.min n.optim df
## All data    19.10      4 38
## Z0          17.43      2 15
## Z1          15.27      1 12
## Z2          19.57      1 11
##
## Resulting formation fractions:
##           ff
## Z0_Z1      1
## Z1_Z2      1
## Z2_sink    1
##
## Estimated disappearance times:
##           DT50  DT90
## Z0 0.3131 1.040
## Z1 1.4543 4.831
## Z2 1.5468 5.138

```

Finally, metabolite Z3 is added to the model. The fit is accelerated by using the starting parameters from the previous fit.

```

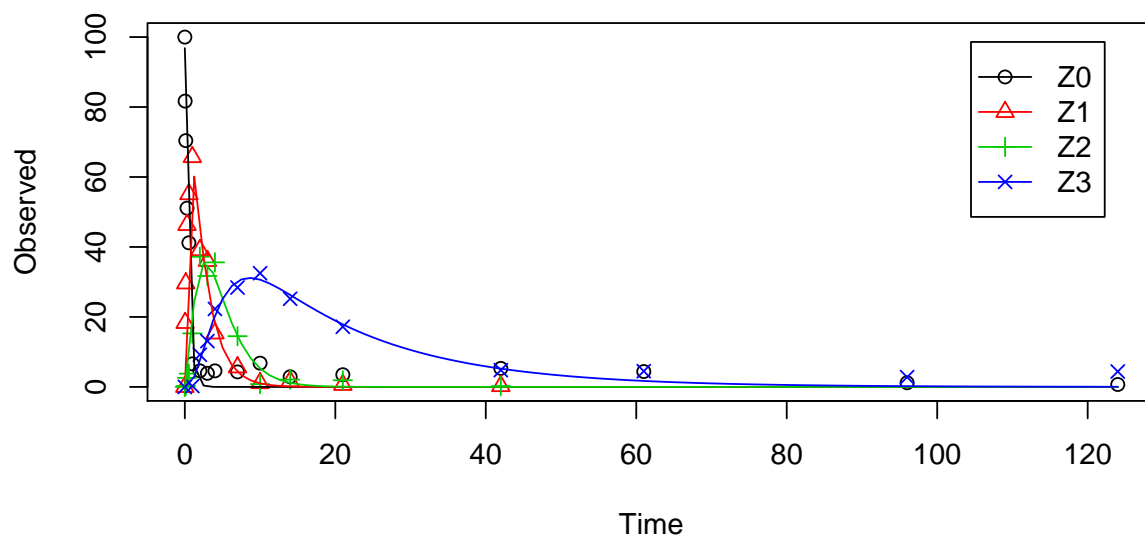
Z.FOCUS <- mkinmod(Z0 = list(type = "SFO", to = "Z1", sink = FALSE),
                  Z1 = list(type = "SFO", to = "Z2", sink = FALSE),

```

```

Z2 = list(type = "SFO", to = "Z3"),
Z3 = list(type = "SFO"))
m.Z.FOCUS <- mkinfit(Z.FOCUS, FOCUS_2006_Z_mkin,
                     quiet = TRUE)
plot(m.Z.FOCUS)

```



```

summary(m.Z.FOCUS, data = FALSE)

## mkin version:      0.9.34
## R version:        3.1.2
## Date of fit:       Fri Nov 21 19:19:18 2014
## Date of summary:   Fri Nov 21 19:19:18 2014
##
## Equations:
## d_Z0 = - 0 - k_Z0_Z1 * Z0
## d_Z1 = + k_Z0_Z1 * Z0 - 0 - k_Z1_Z2 * Z1
## d_Z2 = + k_Z1_Z2 * Z1 - k_Z2_sink * Z2 - k_Z2_Z3 * Z2
## d_Z3 = + k_Z2_Z3 * Z2 - k_Z3_sink * Z3
##
## Model predictions using solution type eigen
##
## Fitted with method Port using 400 model solutions performed in 9.557 s
##
## Weighting: none

```

```

##
## Starting values for parameters to be optimised:
##          value  type
## Z0_0      100.0000  state
## k_Z0_Z1    0.1000 deparm
## k_Z1_Z2    0.1001 deparm
## k_Z2_sink  0.1002 deparm
## k_Z2_Z3    0.1003 deparm
## k_Z3_sink  0.1004 deparm
##
## Starting values for the transformed parameters actually optimised:
##          value lower upper
## Z0_0      100.000000 -Inf  Inf
## log_k_Z0_Z1  -2.302585 -Inf  Inf
## log_k_Z1_Z2  -2.301586 -Inf  Inf
## log_k_Z2_sink -2.300587 -Inf  Inf
## log_k_Z2_Z3  -2.299590 -Inf  Inf
## log_k_Z3_sink -2.298593 -Inf  Inf
##
## Fixed parameter values:
##          value  type
## Z1_0        0  state
## Z2_0        0  state
## Z3_0        0  state
##
## Optimised, transformed parameters:
##          Estimate Std. Error  Lower  Upper t value  Pr(>|t|)
## Z0_0          96.8400    2.05900 92.7100 101.0000  47.040 1.116e-43
## log_k_Z0_Z1     0.7954    0.05332  0.6884   0.9025  14.920 3.078e-20
## log_k_Z1_Z2    -0.7375    0.06123 -0.8605  -0.6146 -12.040 1.569e-16
## log_k_Z2_sink  -1.4330    0.17160 -1.7770  -1.0880  -8.348 4.167e-11
## log_k_Z2_Z3    -1.5470    0.12260 -1.7930  -1.3010 -12.620 2.598e-17
## log_k_Z3_sink  -2.8350    0.24360 -3.3240  -2.3460 -11.640 5.637e-16
##          Pr(>t)
## Z0_0          5.581e-44
## log_k_Z0_Z1    1.539e-20
## log_k_Z1_Z2    7.843e-17
## log_k_Z2_sink  2.084e-11
## log_k_Z2_Z3    1.299e-17
## log_k_Z3_sink  2.819e-16
##
## Parameter correlation:

```

```

##          Z0_0 log_k_Z0_Z1 log_k_Z1_Z2 log_k_Z2_sink
## Z0_0      1.00000    0.05387    0.2727    0.37006
## log_k_Z0_Z1 0.05387    1.00000   -0.0521    0.02443
## log_k_Z1_Z2 0.27275   -0.05210    1.0000    0.29385
## log_k_Z2_sink 0.37006    0.02443    0.2939    1.00000
## log_k_Z2_Z3 -0.07297   -0.03582   -0.1213   -0.18897
## log_k_Z3_sink -0.11349   -0.02522   -0.1915   -0.64299
##          log_k_Z2_Z3 log_k_Z3_sink
## Z0_0      -0.07297   -0.11349
## log_k_Z0_Z1 -0.03582   -0.02522
## log_k_Z1_Z2 -0.12135   -0.19146
## log_k_Z2_sink -0.18897   -0.64299
## log_k_Z2_Z3  1.00000    0.55158
## log_k_Z3_sink  0.55158    1.00000
##
## Residual standard error: 4.1 on 51 degrees of freedom
##
## Backtransformed parameters:
##          Estimate      Lower      Upper
## Z0_0      96.84000 92.71000 101.00000
## k_Z0_Z1    2.21500  1.99100  2.46600
## k_Z1_Z2    0.47830  0.42300  0.54090
## k_Z2_sink  0.23870  0.16910  0.33690
## k_Z2_Z3    0.21290  0.16650  0.27230
## k_Z3_sink  0.05869  0.03599  0.09571
##
## Chi2 error levels in percent:
##          err.min n.optim df
## All data   19.23      6 48
## Z0         17.45      2 15
## Z1         15.24      1 12
## Z2         20.32      2 10
## Z3         11.89      1 11
##
## Resulting formation fractions:
##          ff
## Z0_Z1    1.0000
## Z1_Z2    1.0000
## Z2_sink  0.5285
## Z2_Z3    0.4715
## Z3_sink  1.0000
##

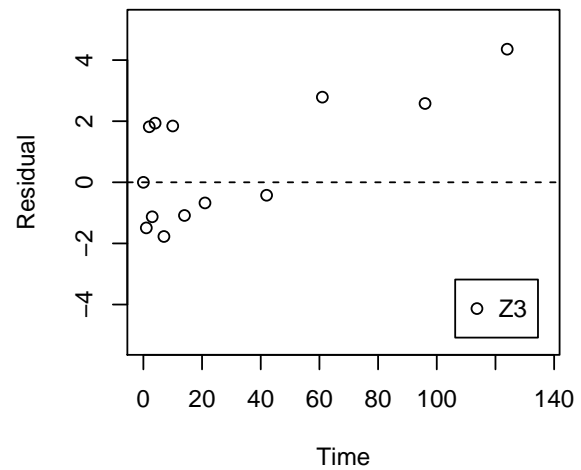
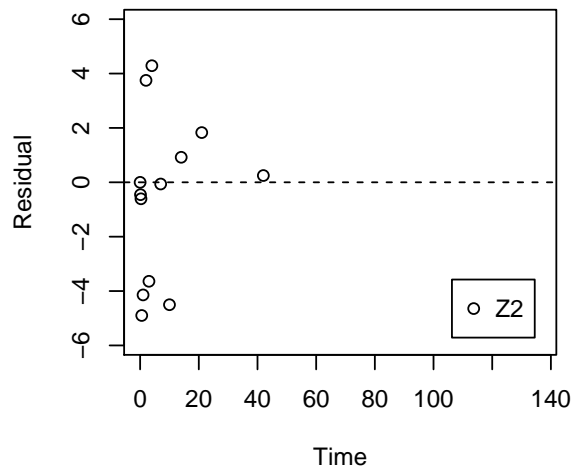
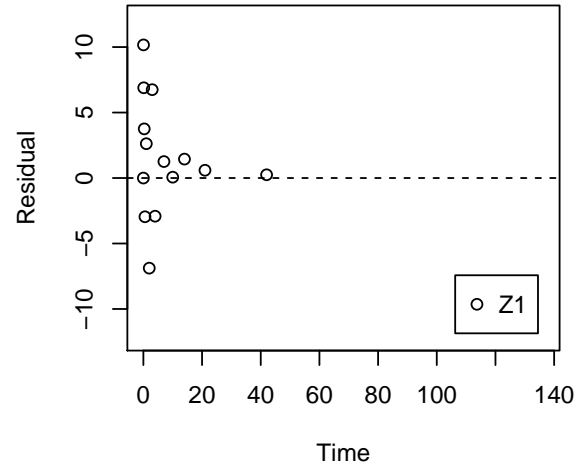
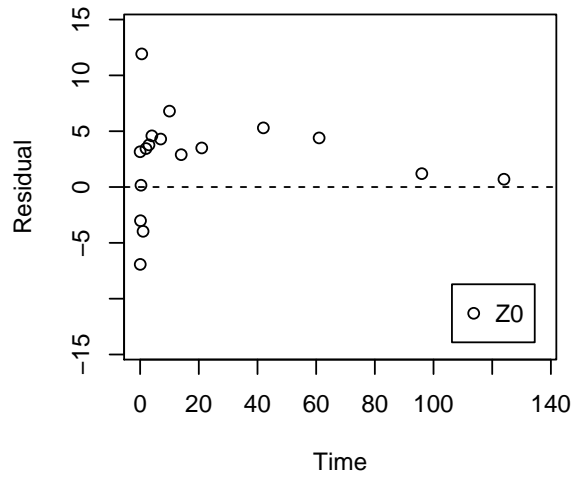
```

```
## Estimated disappearance times:
##      DT50   DT90
## Z0  0.3129  1.039
## Z1  1.4492  4.814
## Z2  1.5348  5.099
## Z3 11.8096 39.231
```

This is the fit corresponding to the final result chosen in Appendix 7 of the FOCUS report. The residual plots can be obtained by

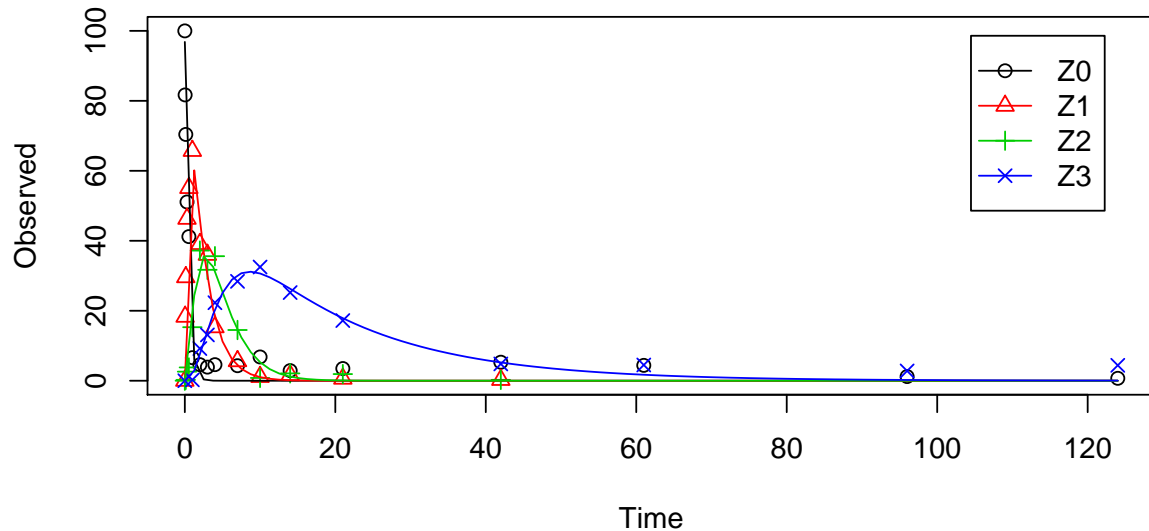
```
par(mfrow = c(2, 2))
mkinresplot(m.Z.FOCUS, "Z0", lpos = "bottomright")
mkinresplot(m.Z.FOCUS, "Z1", lpos = "bottomright")
mkinresplot(m.Z.FOCUS, "Z2", lpos = "bottomright")
mkinresplot(m.Z.FOCUS, "Z3", lpos = "bottomright")
```





We can also investigate the confidence interval for the formation fraction from Z2 to Z3 by specifying the model using formation fractions.

```
Z.FOCUS.ff <- mkinmod(Z0 = list(type = "SFO", to = "Z1", sink = FALSE),
  Z1 = list(type = "SFO", to = "Z2", sink = FALSE),
  Z2 = list(type = "SFO", to = "Z3"),
  Z3 = list(type = "SFO"),
  use_of_ff = "max")
m.Z.FOCUS.ff <- mkinfit(Z.FOCUS.ff, FOCUS_2006_Z_mkin, quiet = TRUE)
plot(m.Z.FOCUS.ff)
```



```
summary(m.Z.FOCUS.ff, data = FALSE)

## mkin version:      0.9.34
## R version:        3.1.2
## Date of fit:       Fri Nov 21 19:19:27 2014
## Date of summary:  Fri Nov 21 19:19:27 2014
##
## Equations:
## d_Z0 = - k_Z0 * Z0
## d_Z1 = + k_Z0 * Z0 - k_Z1 * Z1
## d_Z2 = + k_Z1 * Z1 - k_Z2 * Z2
## d_Z3 = + f_Z2_to_Z3 * k_Z2 * Z2 - k_Z3 * Z3
##
## Model predictions using solution type eigen
##
## Fitted with method Port using 355 model solutions performed in 8.284 s
##
## Weighting: none
##
## Starting values for parameters to be optimised:
##           value  type
## Z0_0       100.0000 state
## k_Z0         0.1000 deparm
## k_Z1         0.1001 deparm
```

```

## k_Z2      0.1002 deparm
## k_Z3      0.1003 deparm
## f_Z2_to_Z3 0.5000 deparm
##
## Starting values for the transformed parameters actually optimised:
##           value lower upper
## Z0_0      100.000000 -Inf   Inf
## log_k_Z0   -2.302585 -Inf   Inf
## log_k_Z1   -2.301586 -Inf   Inf
## log_k_Z2   -2.300587 -Inf   Inf
## log_k_Z3   -2.299590 -Inf   Inf
## f_Z2_ilr_1  0.000000 -Inf   Inf
##
## Fixed parameter values:
##      value  type
## Z1_0      0 state
## Z2_0      0 state
## Z3_0      0 state
##
## Optimised, transformed parameters:
##      Estimate Std. Error  Lower  Upper  t value  Pr(>|t|)
## Z0_0      96.84000    2.05900 92.7100 101.0000  47.0400 1.116e-43
## log_k_Z0    0.79540    0.05332  0.6884  0.9025  14.9200 3.078e-20
## log_k_Z1   -0.73750    0.06123 -0.8605 -0.6146 -12.0400 1.569e-16
## log_k_Z2   -0.79490    0.09790 -0.9915 -0.5984  -8.1200 9.442e-11
## log_k_Z3   -2.83500    0.24360 -3.3240 -2.3460 -11.6400 5.637e-16
## f_Z2_ilr_1 -0.08068    0.16190 -0.4057  0.2443  -0.4983 6.204e-01
##           Pr(>t)
## Z0_0      5.581e-44
## log_k_Z0   1.539e-20
## log_k_Z1   7.844e-17
## log_k_Z2   4.721e-11
## log_k_Z3   2.819e-16
## f_Z2_ilr_1 3.102e-01
##
## Parameter correlation:
##           Z0_0 log_k_Z0 log_k_Z1 log_k_Z2 log_k_Z3 f_Z2_ilr_1
## Z0_0      1.00000  0.053865  0.2727  0.299769 -0.11349  -0.31644
## log_k_Z0   0.05387  1.000000 -0.0521  0.001489 -0.02522  -0.03748
## log_k_Z1   0.27275 -0.052100  1.0000  0.200610 -0.19146  -0.28521
## log_k_Z2   0.29977  0.001489  0.2006  1.000000 -0.27012  -0.38859
## log_k_Z3  -0.11349 -0.025216 -0.1915 -0.270121  1.00000  0.77720

```

```

## f_Z2_ilr_1 -0.31644 -0.037480 -0.2852 -0.388595 0.77720 1.00000
##
## Residual standard error: 4.1 on 51 degrees of freedom
##
## Backtransformed parameters:
##           Estimate      Lower      Upper
## Z0_0          96.84000 92.71000 101.00000
## k_Z0           2.21500 1.99100 2.46600
## k_Z1           0.47830 0.42300 0.54090
## k_Z2           0.45160 0.37100 0.54970
## k_Z3           0.05869 0.03599 0.09571
## f_Z2_to_Z3    0.47150 0.36040 0.58550
##
## Chi2 error levels in percent:
##           err.min n.optim df
## All data    19.23      6 48
## Z0          17.45      2 15
## Z1          15.24      1 12
## Z2          19.61      1 11
## Z3          12.32      2 10
##
## Resulting formation fractions:
##           ff
## Z2_Z3    0.4715
## Z2_sink 0.5285
##
## Estimated disappearance times:
##           DT50   DT90
## Z0 0.3129 1.039
## Z1 1.4492 4.814
## Z2 1.5348 5.099
## Z3 11.8097 39.231

```

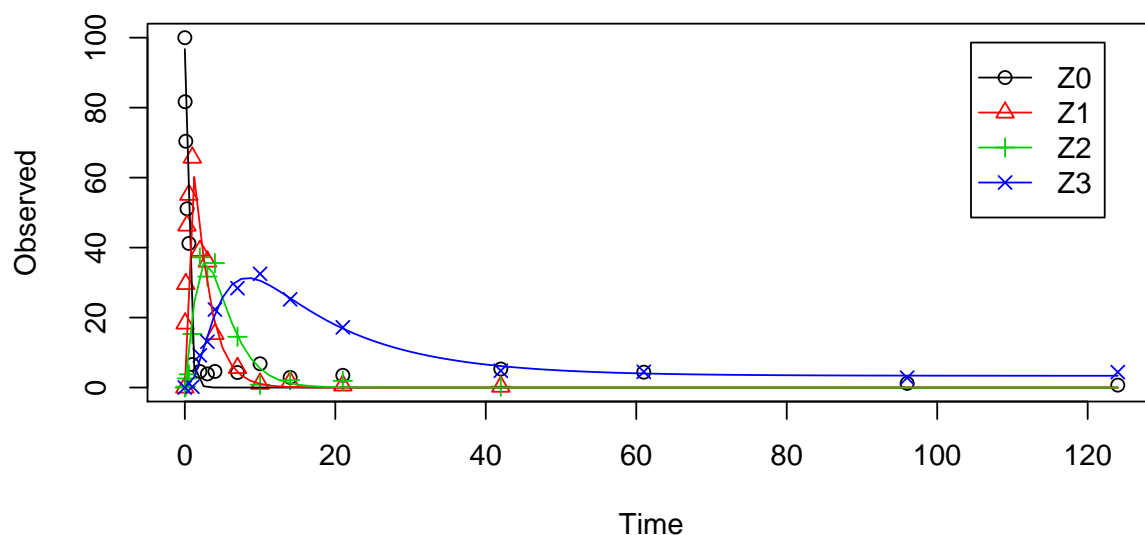
## 4 Using the SFORB model for parent and metabolites

As the FOCUS report states, there is a certain tailing of the time course of metabolite Z3. Also, the time course of the parent compound is not fitted very well using the SFO model, as residues at a certain low level remain.

Therefore, an additional model is offered here, using the single first-order reversible binding (SFORB) model for metabolite Z3. As expected, the  $\chi^2$  error level is lower for metabolite

Z3 using this model and the graphical fit for Z3 is improved. However, the covariance matrix is not returned.

```
Z.mkin.1 <- mkinmod(Z0 = list(type = "SFO", to = "Z1", sink = FALSE),
  Z1 = list(type = "SFO", to = "Z2", sink = FALSE),
  Z2 = list(type = "SFO", to = "Z3"),
  Z3 = list(type = "SFORB"))
m.Z.mkin.1 <- mkinfit(Z.mkin.1, FOCUS_2006_Z_mkin, quiet = TRUE)
plot(m.Z.mkin.1)
```



```
summary(m.Z.mkin.1, data = FALSE)

## mkin version:    0.9.34
## R version:      3.1.2
## Date of fit:     Fri Nov 21 19:19:47 2014
## Date of summary: Fri Nov 21 19:19:47 2014
##
## Equations:
## d_Z0 = - 0 - k_Z0_Z1 * Z0
## d_Z1 = + k_Z0_Z1 * Z0 - 0 - k_Z1_Z2 * Z1
## d_Z2 = + k_Z1_Z2 * Z1 - k_Z2_sink * Z2 - k_Z2_Z3_free * Z2
## d_Z3_free = + k_Z2_Z3_free * Z2 - k_Z3_free_sink * Z3_free -
##             k_Z3_free_bound * Z3_free + k_Z3_bound_free *
##             Z3_bound
## d_Z3_bound = + k_Z3_free_bound * Z3_free - k_Z3_bound_free *
```

```

##          Z3_bound
##
## Model predictions using solution type eigen
##
## Fitted with method Port using 804 model solutions performed in 20.223 s
##
## Weighting: none
##
## Starting values for parameters to be optimised:
##          value  type
## Z0_0          100.0000  state
## k_Z0_Z1         0.1000 deparm
## k_Z1_Z2         0.1001 deparm
## k_Z2_sink        0.1002 deparm
## k_Z2_Z3_free     0.1003 deparm
## k_Z3_free_sink   0.1004 deparm
## k_Z3_free_bound  0.1000 deparm
## k_Z3_bound_free  0.0200 deparm
##
## Starting values for the transformed parameters actually optimised:
##          value lower upper
## Z0_0          100.000000  -Inf  Inf
## log_k_Z0_Z1    -2.302585  -Inf  Inf
## log_k_Z1_Z2    -2.301586  -Inf  Inf
## log_k_Z2_sink  -2.300587  -Inf  Inf
## log_k_Z2_Z3_free -2.299590  -Inf  Inf
## log_k_Z3_free_sink -2.298593  -Inf  Inf
## log_k_Z3_free_bound -2.302585  -Inf  Inf
## log_k_Z3_bound_free -3.912023  -Inf  Inf
##
## Fixed parameter values:
##          value  type
## Z1_0          0  state
## Z2_0          0  state
## Z3_free_0      0  state
## Z3_bound_0     0  state
##
## Optimised, transformed parameters:
##          Estimate Std. Error Lower Upper t value Pr(>|t|)
## Z0_0          96.7400         NA     NA     NA     NA     NA
## log_k_Z0_Z1     0.7947         NA     NA     NA     NA     NA
## log_k_Z1_Z2    -0.7426         NA     NA     NA     NA     NA

```

```

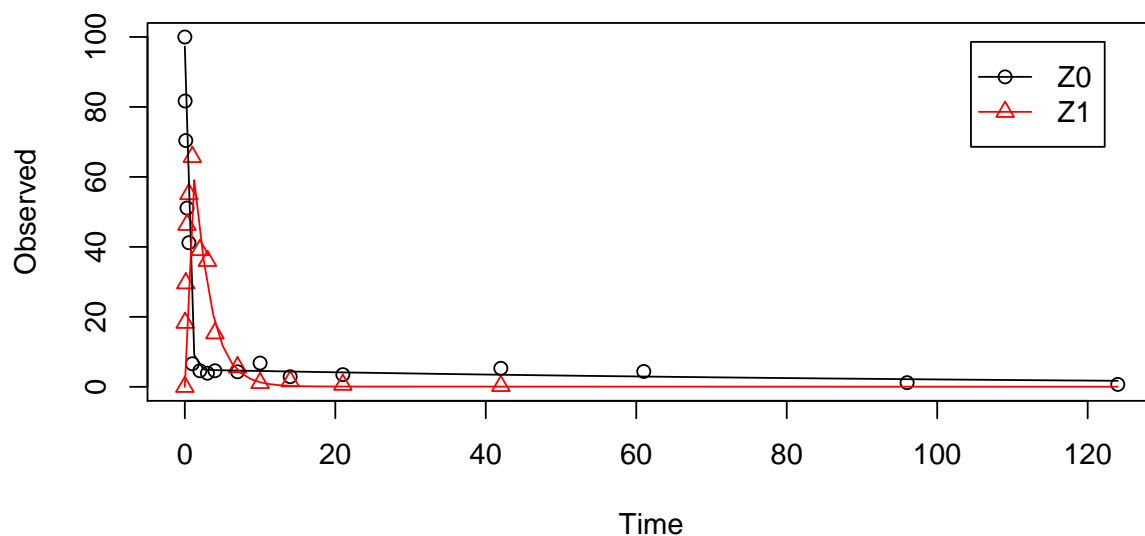
## log_k_Z2_sink      -1.4950      NA      NA      NA      NA      NA
## log_k_Z2_Z3_free   -1.5040      NA      NA      NA      NA      NA
## log_k_Z3_free_sink -2.6540      NA      NA      NA      NA      NA
## log_k_Z3_free_bound -5.2440      NA      NA      NA      NA      NA
## log_k_Z3_bound_free -22.1700     NA      NA      NA      NA      NA
##                      Pr(>t)
## Z0_0                NA
## log_k_Z0_Z1         NA
## log_k_Z1_Z2         NA
## log_k_Z2_sink       NA
## log_k_Z2_Z3_free    NA
## log_k_Z3_free_sink  NA
## log_k_Z3_free_bound NA
## log_k_Z3_bound_free NA
##
## Parameter correlation:
## Could not estimate covariance matrix; singular system:
##
## Residual standard error: 4.107 on 49 degrees of freedom
##
## Backtransformed parameters:
##              Estimate Lower Upper
## Z0_0          9.674e+01    NA    NA
## k_Z0_Z1        2.214e+00    NA    NA
## k_Z1_Z2        4.759e-01    NA    NA
## k_Z2_sink      2.243e-01    NA    NA
## k_Z2_Z3_free   2.222e-01    NA    NA
## k_Z3_free_sink  7.034e-02    NA    NA
## k_Z3_free_bound 5.279e-03    NA    NA
## k_Z3_bound_free 2.358e-10    NA    NA
##
## Chi2 error levels in percent:
##              err.min n.optim df
## All data    19.406      8 47
## Z0           17.429      2 15
## Z1           15.275      1 12
## Z2           20.279      2 10
## Z3            8.562      3 10
##
## Estimated Eigenvalues of SFORB model(s):
##      Z3_b1      Z3_b2
## 7.562e-02 2.194e-10

```

```
##
## Resulting formation fractions:
##          ff
## Z0_Z1      1.0000
## Z1_Z2      1.0000
## Z2_sink    0.5024
## Z2_Z3_free 0.4976
## Z3_free_sink 1.0000
##
## Estimated disappearance times:
##      DT50  DT90 DT50_Z3_b1 DT50_Z3_b2
## Z0  0.3131  1.040          NA          NA
## Z1  1.4566  4.839          NA          NA
## Z2  1.5523  5.157          NA          NA
## Z3 10.1978 45.329          9.166  3.16e+09
```

Therefore, a further stepwise model building is performed starting from the stage of parent and one metabolite, starting from the assumption that the model fit for the parent compound can be improved by using the SFORB model.

```
Z.mkin.2 <- mkinmod(Z0 = list(type = "SFORB", to = "Z1", sink = FALSE),
                    Z1 = list(type = "SFO"))
m.Z.mkin.2 <- mkinfit(Z.mkin.2, FOCUS_2006_Z_mkin, quiet = TRUE)
plot(m.Z.mkin.2)
```





```

summary(m.Z.mkin.2, data = FALSE)

## mkin version:      0.9.34
## R version:         3.1.2
## Date of fit:        Fri Nov 21 19:19:50 2014
## Date of summary:    Fri Nov 21 19:19:50 2014
##
## Equations:
## d_Z0_free = - 0 - k_Z0_free_bound * Z0_free + k_Z0_bound_free
##              * Z0_bound - k_Z0_free_Z1 * Z0_free
## d_Z0_bound = + k_Z0_free_bound * Z0_free - k_Z0_bound_free *
##              Z0_bound
## d_Z1 = + k_Z0_free_Z1 * Z0_free - k_Z1_sink * Z1
##
## Model predictions using solution type eigen
##
## Fitted with method Port using 149 model solutions performed in 2.046 s
##
## Weighting: none
##
## Starting values for parameters to be optimised:
##              value  type
## Z0_free_0      100.0000  state
## k_Z0_free_bound  0.1000 deparm
## k_Z0_bound_free  0.0200 deparm
## k_Z0_free_Z1     0.1002 deparm
## k_Z1_sink        0.1003 deparm
##
## Starting values for the transformed parameters actually optimised:
##              value lower upper
## Z0_free_0      100.000000  -Inf  Inf
## log_k_Z0_free_bound -2.302585  -Inf  Inf
## log_k_Z0_bound_free -3.912023  -Inf  Inf
## log_k_Z0_free_Z1    -2.300587  -Inf  Inf
## log_k_Z1_sink       -2.299590  -Inf  Inf
##
## Fixed parameter values:
##              value  type
## Z0_bound_0        0  state
## Z1_0               0  state
##
## Optimised, transformed parameters:

```

```

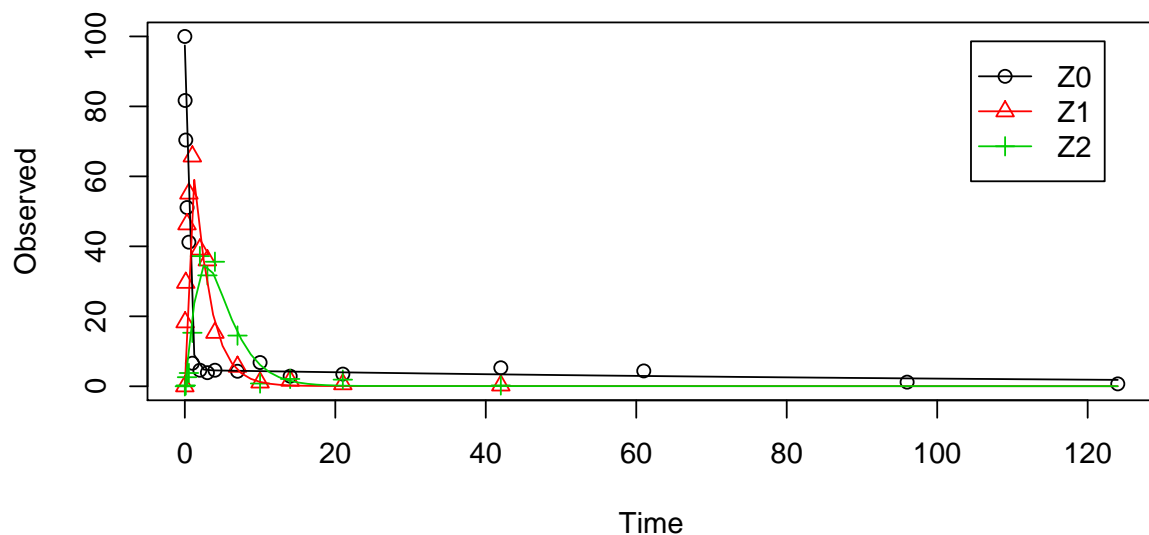
##               Estimate Std. Error   Lower   Upper t value
## Z0_free_0         97.2900    2.39500 92.3600 102.2000 40.610
## log_k_Z0_free_bound -2.0820    0.43220 -2.9710 -1.1940 -4.818
## log_k_Z0_bound_free -4.7200    1.60500 -8.0190 -1.4210 -2.941
## log_k_Z0_free_Z1      0.8549    0.06430  0.7227  0.9871 13.300
## log_k_Z1_sink       -0.7934    0.08506 -0.9682 -0.6185 -9.327
##               Pr(>|t|)   Pr(>t)
## Z0_free_0         4.728e-25 2.364e-25
## log_k_Z0_free_bound 5.440e-05 2.720e-05
## log_k_Z0_bound_free 6.785e-03 3.393e-03
## log_k_Z0_free_Z1    4.185e-13 2.092e-13
## log_k_Z1_sink       8.860e-10 4.430e-10
##
## Parameter correlation:
##               Z0_free_0 log_k_Z0_free_bound log_k_Z0_bound_free
## Z0_free_0         1.000000             0.006492             0.03324
## log_k_Z0_free_bound 0.006492             1.000000             0.54647
## log_k_Z0_bound_free 0.033236             0.546472             1.00000
## log_k_Z0_free_Z1    0.111818             0.413920             0.15837
## log_k_Z1_sink       0.391554             -0.291910            -0.12597
##               log_k_Z0_free_Z1 log_k_Z1_sink
## Z0_free_0         0.11182             0.39155
## log_k_Z0_free_bound 0.41392            -0.29191
## log_k_Z0_bound_free 0.15837            -0.12597
## log_k_Z0_free_Z1    1.00000            -0.04187
## log_k_Z1_sink       -0.04187             1.00000
##
## Residual standard error: 4.438 on 26 degrees of freedom
##
## Backtransformed parameters:
##               Estimate   Lower   Upper
## Z0_free_0         97.290000 92.360000 102.2000
## k_Z0_free_bound    0.124700 0.051280  0.3031
## k_Z0_bound_free     0.008912 0.000329  0.2414
## k_Z0_free_Z1       2.351000 2.060000  2.6830
## k_Z1_sink          0.452300 0.379800  0.5387
##
## Chi2 error levels in percent:
##               err.min n.optim df
## All data      15.63      5 25
## Z0             14.74      4 13
## Z1             14.31      1 12

```

```
##
## Estimated Eigenvalues of SFORB model(s):
##      Z0_b1      Z0_b2
## 2.476315 0.008462
##
## Resulting formation fractions:
##           ff
## Z0_free_Z1  1
## Z1_sink      1
##
## Estimated disappearance times:
##      DT50  DT90  DT50_Z0_b1  DT50_Z0_b2
## Z0 0.302 1.190      0.2799      81.92
## Z1 1.532 5.091          NA          NA
```

When metabolite Z2 is added, the additional sink for Z1 is turned off again, for the same reasons as in the original analysis.

```
Z.mkin.3 <- mkinmod(Z0 = list(type = "SFORB", to = "Z1", sink = FALSE),
                  Z1 = list(type = "SFO", to = "Z2", sink = FALSE),
                  Z2 = list(type = "SFO"))
m.Z.mkin.3 <- mkinfit(Z.mkin.3, FOCUS_2006_Z_mkin, quiet = TRUE)
plot(m.Z.mkin.3)
```



```

summary(m.Z.mkin.3, data = FALSE)

## mkin version:      0.9.34
## R version:        3.1.2
## Date of fit:       Fri Nov 21 19:19:56 2014
## Date of summary:  Fri Nov 21 19:19:56 2014
##
## Equations:
## d_Z0_free = - 0 - k_Z0_free_bound * Z0_free + k_Z0_bound_free
##              * Z0_bound - k_Z0_free_Z1 * Z0_free
## d_Z0_bound = + k_Z0_free_bound * Z0_free - k_Z0_bound_free *
##              Z0_bound
## d_Z1 = + k_Z0_free_Z1 * Z0_free - 0 - k_Z1_Z2 * Z1
## d_Z2 = + k_Z1_Z2 * Z1 - k_Z2_sink * Z2
##
## Model predictions using solution type eigen
##
## Fitted with method Port using 337 model solutions performed in 6.473 s
##
## Weighting: none
##
## Starting values for parameters to be optimised:
##              value    type
## Z0_free_0      100.0000 state
## k_Z0_free_bound  0.1000 deparm
## k_Z0_bound_free  0.0200 deparm
## k_Z0_free_Z1     0.1002 deparm
## k_Z1_Z2          0.1003 deparm
## k_Z2_sink        0.1004 deparm
##
## Starting values for the transformed parameters actually optimised:
##              value lower upper
## Z0_free_0      100.000000 -Inf  Inf
## log_k_Z0_free_bound -2.302585 -Inf  Inf
## log_k_Z0_bound_free -3.912023 -Inf  Inf
## log_k_Z0_free_Z1    -2.300587 -Inf  Inf
## log_k_Z1_Z2         -2.299590 -Inf  Inf
## log_k_Z2_sink       -2.298593 -Inf  Inf
##
## Fixed parameter values:
##              value    type
## Z0_bound_0       0 state

```

```

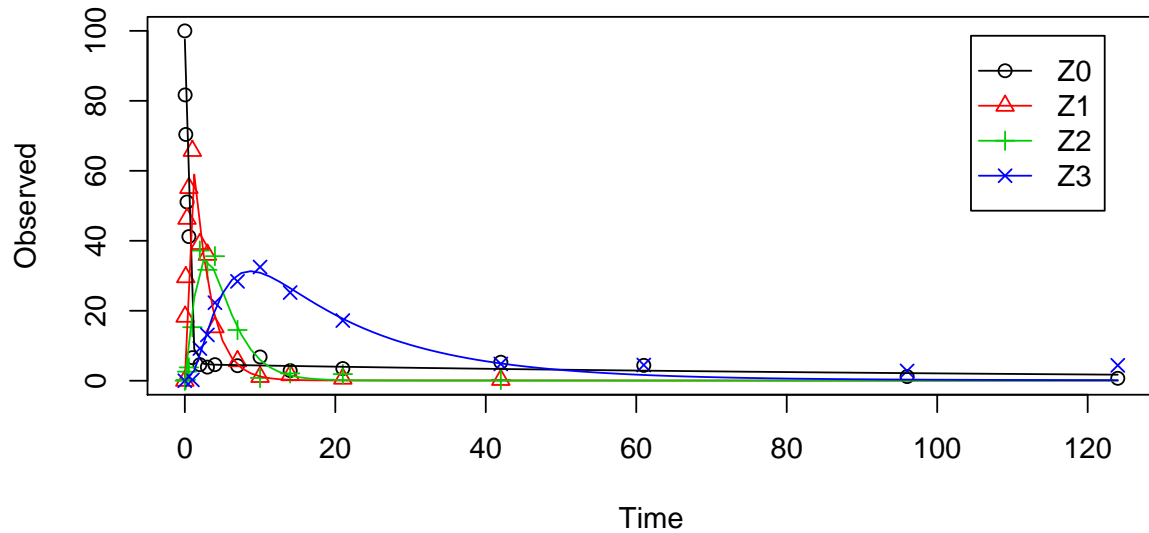
## Z1_0          0 state
## Z2_0          0 state
##
## Optimised, transformed parameters:
##           Estimate Std. Error   Lower   Upper t value
## Z0_free_0      97.4400    2.07100 93.2400 101.6000 47.050
## log_k_Z0_free_bound -2.1490    0.40400 -2.9670 -1.3310 -5.319
## log_k_Z0_bound_free -4.8380    1.61100 -8.1000 -1.5770 -3.003
## log_k_Z0_free_Z1     0.8457    0.05831  0.7277  0.9638 14.500
## log_k_Z1_Z2     -0.7812    0.06485 -0.9125 -0.6499 -12.050
## log_k_Z2_sink     -0.8606    0.10570 -1.0750 -0.6466 -8.140
##           Pr(>|t|)   Pr(>t)
## Z0_free_0      2.697e-35 1.348e-35
## log_k_Z0_free_bound 4.880e-06 2.440e-06
## log_k_Z0_bound_free 4.708e-03 2.354e-03
## log_k_Z0_free_Z1   4.501e-17 2.251e-17
## log_k_Z1_Z2        1.522e-14 7.611e-15
## log_k_Z2_sink       7.465e-10 3.732e-10
##
## Parameter correlation:
##           Z0_free_0 log_k_Z0_free_bound log_k_Z0_bound_free
## Z0_free_0      1.00000           0.07502           0.07080
## log_k_Z0_free_bound 0.07502           1.00000           0.54254
## log_k_Z0_bound_free 0.07080           0.54254           1.00000
## log_k_Z0_free_Z1   0.09079           0.42453           0.16315
## log_k_Z1_Z2        0.25718           -0.22757          -0.08626
## log_k_Z2_sink       0.28877           -0.21050          -0.07922
##           log_k_Z0_free_Z1 log_k_Z1_Z2 log_k_Z2_sink
## Z0_free_0      0.09079      0.25718      0.28877
## log_k_Z0_free_bound 0.42453     -0.22757     -0.21050
## log_k_Z0_bound_free 0.16315     -0.08626     -0.07922
## log_k_Z0_free_Z1   1.00000     -0.10084     -0.04901
## log_k_Z1_Z2       -0.10084      1.00000      0.27278
## log_k_Z2_sink     -0.04901      0.27278      1.00000
##
## Residual standard error: 4.081 on 38 degrees of freedom
##
## Backtransformed parameters:
##           Estimate   Lower   Upper
## Z0_free_0      97.44000 9.324e+01 101.6000
## k_Z0_free_bound  0.11660 5.148e-02  0.2642
## k_Z0_bound_free  0.00792 3.036e-04  0.2066

```

```
## k_Z0_free_Z1      2.33000 2.070e+00  2.6220
## k_Z1_Z2           0.45790 4.015e-01  0.5221
## k_Z2_sink         0.42290 3.414e-01  0.5238
##
## Chi2 error levels in percent:
##           err.min n.optim df
## All data   17.33      6 36
## Z0         14.67      4 13
## Z1         14.41      1 12
## Z2         20.29      1 11
##
## Estimated Eigenvalues of SFORB model(s):
##      Z0_b1      Z0_b2
## 2.446638 0.007542
##
## Resulting formation fractions:
##           ff
## Z0_free_Z1  1
## Z1_Z2        1
## Z2_sink      1
##
## Estimated disappearance times:
##      DT50  DT90 DT50_Z0_b1 DT50_Z0_b2
## Z0 0.3043 1.185      0.2833      91.91
## Z1 1.5138 5.029          NA          NA
## Z2 1.6391 5.445          NA          NA
```

This results in a much better representation of the behaviour of the parent compound Z0. Finally, Z3 is added as well. These models appear overparameterised (no covariance matrix returned) if the sink for Z1 is left in the models.

```
Z.mkin.4 <- mkinmod(Z0 = list(type = "SFORB", to = "Z1", sink = FALSE),
                  Z1 = list(type = "SFO", to = "Z2", sink = FALSE),
                  Z2 = list(type = "SFO", to = "Z3"),
                  Z3 = list(type = "SFO"))
m.Z.mkin.4 <- mkinfit(Z.mkin.4, FOCUS_2006_Z_mkin,
                    quiet = TRUE)
plot(m.Z.mkin.4)
```



```
summary(m.Z.mkin.4, data = FALSE)

## mkin version:      0.9.34
## R version:         3.1.2
## Date of fit:        Fri Nov 21 19:20:09 2014
## Date of summary:    Fri Nov 21 19:20:09 2014
##
## Equations:
## d_Z0_free = - 0 - k_Z0_free_bound * Z0_free + k_Z0_bound_free
##              * Z0_bound - k_Z0_free_Z1 * Z0_free
## d_Z0_bound = + k_Z0_free_bound * Z0_free - k_Z0_bound_free *
##              Z0_bound
## d_Z1 = + k_Z0_free_Z1 * Z0_free - 0 - k_Z1_Z2 * Z1
## d_Z2 = + k_Z1_Z2 * Z1 - k_Z2_sink * Z2 - k_Z2_Z3 * Z2
## d_Z3 = + k_Z2_Z3 * Z2 - k_Z3_sink * Z3
##
## Model predictions using solution type eigen
##
## Fitted with method Port using 531 model solutions performed in 12.958 s
##
## Weighting: none
##
## Starting values for parameters to be optimised:
##              value      type
```

```

## Z0_free_0      100.0000  state
## k_Z0_free_bound  0.1000 deparm
## k_Z0_bound_free  0.0200 deparm
## k_Z0_free_Z1     0.1002 deparm
## k_Z1_Z2          0.1003 deparm
## k_Z2_sink        0.1004 deparm
## k_Z2_Z3          0.1005 deparm
## k_Z3_sink        0.1006 deparm
##
## Starting values for the transformed parameters actually optimised:
##
##               value lower upper
## Z0_free_0      100.000000  -Inf  Inf
## log_k_Z0_free_bound -2.302585  -Inf  Inf
## log_k_Z0_bound_free -3.912023  -Inf  Inf
## log_k_Z0_free_Z1   -2.300587  -Inf  Inf
## log_k_Z1_Z2        -2.299590  -Inf  Inf
## log_k_Z2_sink      -2.298593  -Inf  Inf
## log_k_Z2_Z3        -2.297598  -Inf  Inf
## log_k_Z3_sink      -2.296603  -Inf  Inf
##
## Fixed parameter values:
##               value type
## Z0_bound_0      0 state
## Z1_0            0 state
## Z2_0            0 state
## Z3_0            0 state
##
## Optimised, transformed parameters:
##               Estimate Std. Error  Lower  Upper t value
## Z0_free_0      97.5300    1.88700  93.7400 101.3000  51.700
## log_k_Z0_free_bound -2.1360    0.36810 -2.8760  -1.3960  -5.803
## log_k_Z0_bound_free -4.7650    1.41800 -7.6140  -1.9160  -3.362
## log_k_Z0_free_Z1     0.8470    0.05339  0.7398   0.9543  15.860
## log_k_Z1_Z2        -0.7769    0.05834 -0.8942  -0.6597 -13.320
## log_k_Z2_sink      -1.5610    0.18260 -1.9280  -1.1940  -8.550
## log_k_Z2_Z3        -1.5280    0.11350 -1.7560  -1.2990 -13.450
## log_k_Z3_sink      -2.7690    0.22460 -3.2200  -2.3180 -12.330
##               Pr(>|t|)  Pr(>t)
## Z0_free_0      2.066e-44 1.033e-44
## log_k_Z0_free_bound 4.709e-07 2.354e-07
## log_k_Z0_bound_free 1.510e-03 7.548e-04
## log_k_Z0_free_Z1   6.130e-21 3.065e-21

```



```

## log_k_Z1_Z2      6.658e-18 3.329e-18
## log_k_Z2_sink    2.793e-11 1.396e-11
## log_k_Z2_Z3      4.487e-18 2.244e-18
## log_k_Z3_sink    1.246e-16 6.232e-17
##
## Parameter correlation:
##              Z0_free_0 log_k_Z0_free_bound log_k_Z0_bound_free
## Z0_free_0      1.00000      0.07822      0.06921
## log_k_Z0_free_bound 0.07822      1.00000      0.53978
## log_k_Z0_bound_free 0.06921      0.53978      1.00000
## log_k_Z0_free_Z1  0.08882      0.42765      0.16280
## log_k_Z1_Z2      0.24238     -0.22742     -0.08936
## log_k_Z2_sink    0.32993     -0.26331     -0.12744
## log_k_Z2_Z3     -0.07494      0.06698      0.06082
## log_k_Z3_sink    -0.10456      0.13844      0.12525
##              log_k_Z0_free_Z1 log_k_Z1_Z2 log_k_Z2_sink
## Z0_free_0      0.08882      0.24238      0.32993
## log_k_Z0_free_bound 0.42765     -0.22742     -0.26331
## log_k_Z0_bound_free 0.16280     -0.08936     -0.12744
## log_k_Z0_free_Z1  1.00000     -0.10841     -0.05309
## log_k_Z1_Z2     -0.10841      1.00000      0.34052
## log_k_Z2_sink   -0.05309      0.34052      1.00000
## log_k_Z2_Z3     -0.01281     -0.14885     -0.25473
## log_k_Z3_sink    0.01857     -0.22486     -0.68320
##              log_k_Z2_Z3 log_k_Z3_sink
## Z0_free_0     -0.07494     -0.10456
## log_k_Z0_free_bound 0.06698      0.13844
## log_k_Z0_bound_free 0.06082      0.12525
## log_k_Z0_free_Z1 -0.01281      0.01857
## log_k_Z1_Z2     -0.14885     -0.22486
## log_k_Z2_sink   -0.25473     -0.68320
## log_k_Z2_Z3      1.00000      0.56390
## log_k_Z3_sink    0.56390      1.00000
##
## Residual standard error: 3.737 on 49 degrees of freedom
##
## Backtransformed parameters:
##              Estimate      Lower      Upper
## Z0_free_0      97.530000 9.374e+01 101.3000
## k_Z0_free_bound 0.118100 5.636e-02 0.2475
## k_Z0_bound_free 0.008522 4.936e-04 0.1471
## k_Z0_free_Z1    2.333000 2.095e+00 2.5970

```

```

## k_Z1_Z2      0.459800 4.089e-01  0.5170
## k_Z2_sink    0.209900 1.455e-01  0.3030
## k_Z2_Z3      0.217000 1.728e-01  0.2727
## k_Z3_sink    0.062720 3.994e-02  0.0985
##
## Chi2 error levels in percent:
##           err.min n.optim df
## All data   17.50      8 46
## Z0         14.69      4 13
## Z1         14.39      1 12
## Z2         21.05      2 10
## Z3         11.76      1 11
##
## Estimated Eigenvalues of SFORB model(s):
##   Z0_b1  Z0_b2
## 2.45127 0.00811
##
## Resulting formation fractions:
##           ff
## Z0_free_Z1 1.0000
## Z1_Z2      1.0000
## Z2_sink    0.4917
## Z2_Z3      0.5083
## Z3_sink    1.0000
##
## Estimated disappearance times:
##      DT50  DT90 DT50_Z0_b1 DT50_Z0_b2
## Z0  0.304  1.186      0.2828      85.47
## Z1  1.507  5.008          NA          NA
## Z2  1.623  5.393          NA          NA
## Z3 11.051 36.712          NA          NA

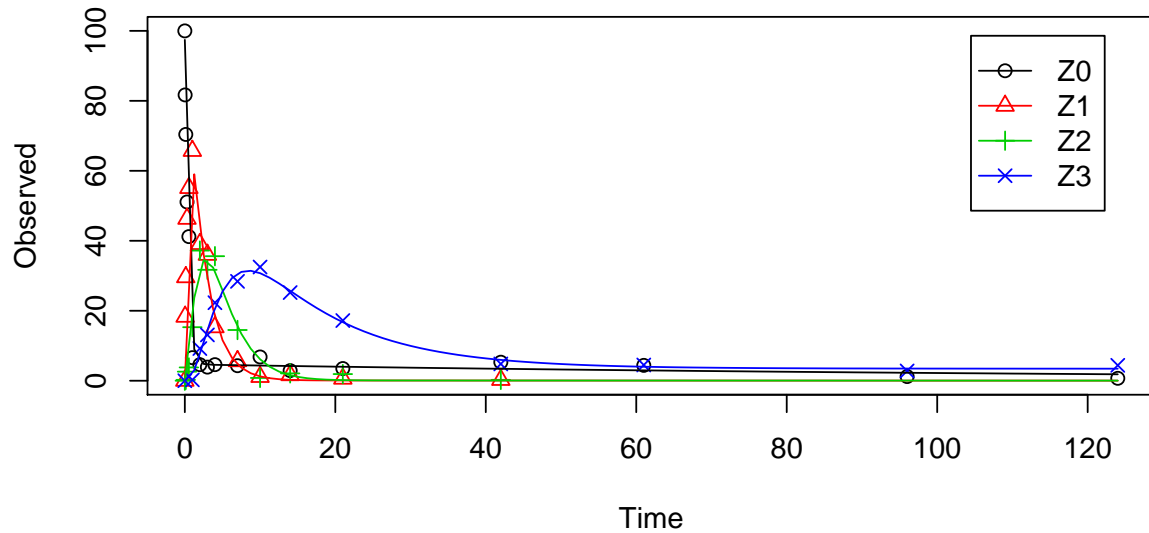
```

The error level of the fit, but especially of metabolite Z3, can be improved if the SFORB model is chosen for this metabolite, as this model is capable of representing the tailing of the metabolite decline phase.

```

Z.mkin.5 <- mkinmod(Z0 = list(type = "SFORB", to = "Z1", sink = FALSE),
                  Z1 = list(type = "SFO", to = "Z2", sink = FALSE),
                  Z2 = list(type = "SFO", to = "Z3"),
                  Z3 = list(type = "SFORB"))
m.Z.mkin.5 <- mkinfit(Z.mkin.5, FOCUS_2006_Z_mkin, quiet = TRUE)
plot(m.Z.mkin.5)

```



```
summary(m.Z.mkin.5, data = FALSE)$bpar
```

##		Estimate	Lower	Upper
##	Z0_free_0	9.742495e+01	NA	NA
##	k_Z0_free_bound	1.167578e-01	NA	NA
##	k_Z0_bound_free	7.890227e-03	NA	NA
##	k_Z0_free_Z1	2.330001e+00	NA	NA
##	k_Z1_Z2	4.575901e-01	NA	NA
##	k_Z2_sink	1.957094e-01	NA	NA
##	k_Z2_Z3_free	2.265847e-01	NA	NA
##	k_Z3_free_sink	7.478923e-02	NA	NA
##	k_Z3_free_bound	5.217941e-03	NA	NA
##	k_Z3_bound_free	2.124871e-10	NA	NA

The summary view of the backtransformed parameters shows that we get no confidence intervals due to overparameterisation. As the optimized `k_Z3_bound_free` is excessively small, it seems reasonable to fix it to zero.

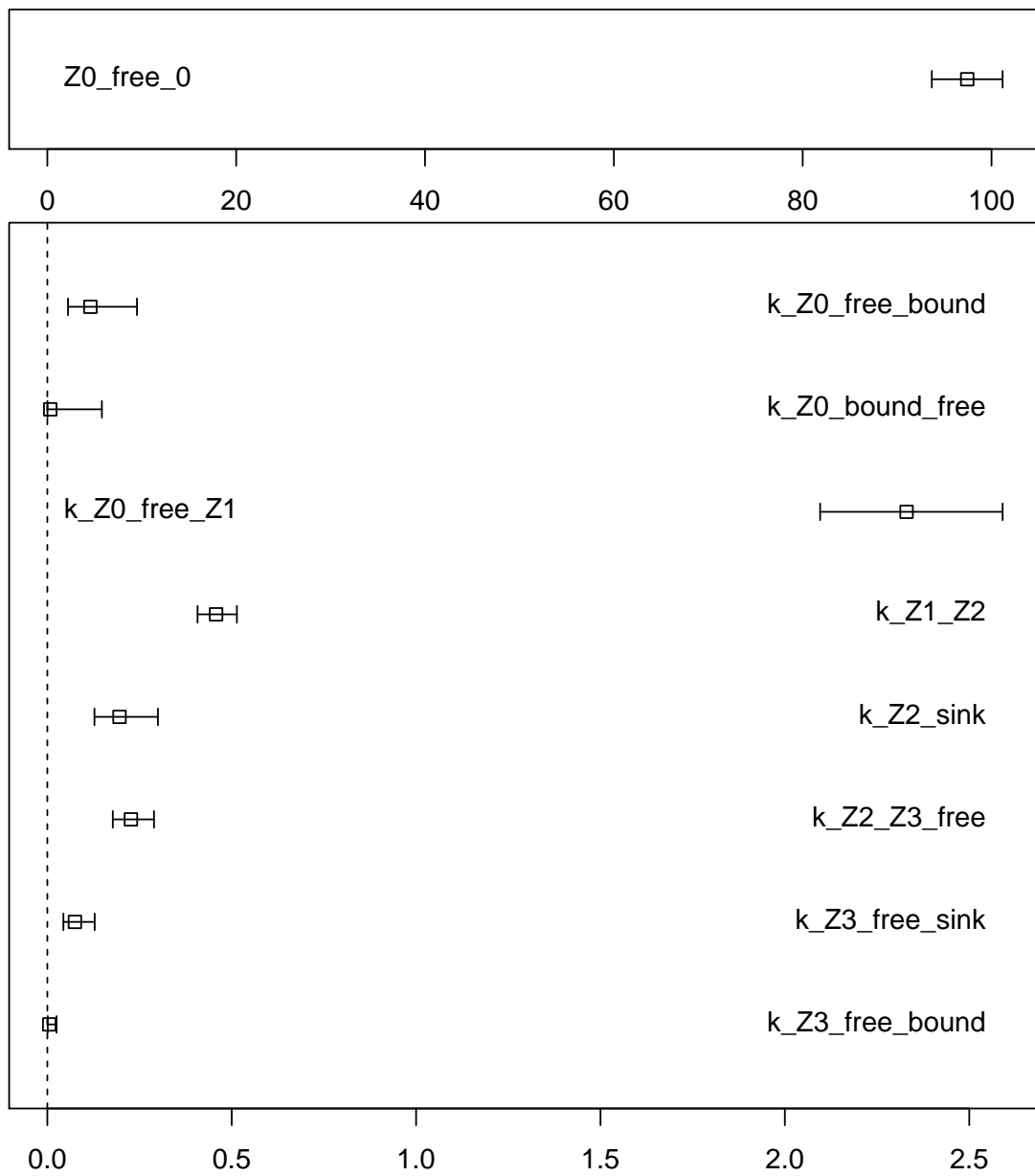
```
m.Z.mkin.5a <- mkinfit(Z.mkin.5, FOCUS_2006_Z_mkin,
  parms.ini = c(k_Z3_bound_free = 0),
  fixed_parms = "k_Z3_bound_free",
  quiet = TRUE)
summary(m.Z.mkin.5a, data = FALSE)$bpar
```

##		Estimate	Lower	Upper
----	--	----------	-------	-------

```
## Z0_free_0      97.424951441 9.367615e+01 101.17374975
## k_Z0_free_bound 0.116757743 5.608481e-02  0.24306708
## k_Z0_bound_free 0.007890254 4.209026e-04  0.14791097
## k_Z0_free_Z1   2.330000647 2.095695e+00  2.59050229
## k_Z1_Z2        0.457590216 4.073552e-01  0.51402026
## k_Z2_sink      0.195709289 1.277412e-01  0.29984148
## k_Z2_Z3_free   0.226584870 1.775283e-01  0.28919721
## k_Z3_free_sink  0.074789319 4.353592e-02  0.12847879
## k_Z3_free_bound 0.005217940 1.092645e-03  0.02491835
```

A graphical representation of the confidence intervals can finally be obtained.

```
mkinpaplot(m.Z.mkin.5a)
```



The endpoints obtained with this model are

```
endpoints(m.Z.mkin.5a)

## $ff
##   Z0_free_Z1      Z1_Z2      Z2_sink      Z2_Z3_free      Z3_free_sink
##   1.000000      1.000000      0.463443      0.536557      1.000000
##
## $SFORB
##      Z0_b1      Z0_b2      Z3_b1      Z3_b2
## 2.447136068 0.007512577 0.080007259 0.000000000
```

```
##
## $distimes
##          DT50          DT90 DT50_Z0_b1 DT50_Z0_b2 DT50_Z3_b1 DT50_Z3_b2
## Z0 0.3043058  1.184811  0.2832483   92.26491          NA          NA
## Z1 1.5147771  5.031981          NA          NA          NA          NA
## Z2 1.6413847  5.452562          NA          NA          NA          NA
## Z3 9.5674970 41.136541          NA          NA   8.663554          Inf
```

It is clear the degradation rate of Z3 towards the end of the experiment is very low as DT50\_Z3\_b2 is reported to be infinity. However, this appears to be a feature of the data.

```
par(mfrow = c(2, 2))
mkinresplot(m.Z.mkin.5, "Z0", lpos = "bottomright")
mkinresplot(m.Z.mkin.5, "Z1", lpos = "bottomright")
mkinresplot(m.Z.mkin.5, "Z2", lpos = "bottomright")
mkinresplot(m.Z.mkin.5, "Z3", lpos = "bottomright")
```



As expected, the residual plots are much more random than in the case of the all SFO model for which they were shown above. In conclusion, the model `Z.mkin.5` is proposed as the best-fit model for the dataset from Appendix 7 of the FOCUS report.

## References

FOCUS Work Group on Degradation Kinetics. *Generic guidance for estimating persistence and degradation kinetics from environmental fate studies on pesticides in EU registration*, 1.0 edition, November 2011. URL <http://focus.jrc.ec.europa.eu/dk>.